

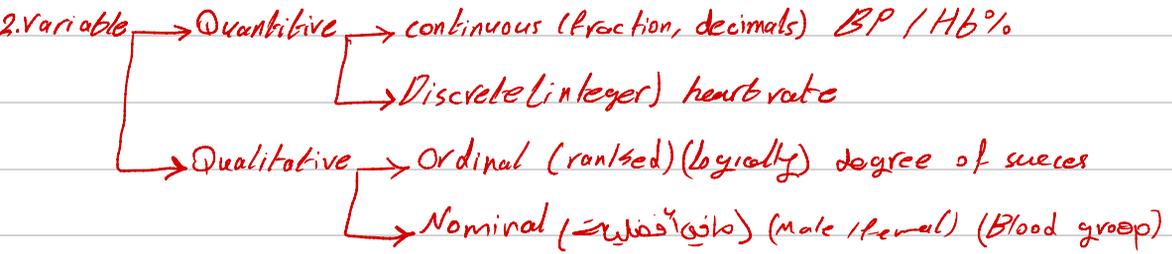


Biostatistics...

Med

- Type of data :

1. constant → عدد معين



- Measures of central tendency :

1. Mean = average = $\frac{\sum X}{n} = \bar{X}$

2. Median = middle value (order from lower to upper value)

→ above 50% below 50% #
أفضل طريقة لقياس أرقام كبيرة أو صغيرة
ما يتأثر بقيمة القيمة الكبيرة مثل Mean

3. Mode = most frequent (يمكن أن يكون أكثر من رقم)

- Measures of dispersion :

1. Range → largest - smallest values.

2. Interquartile range → $Q_3 - Q_1$ (25th - 75th)

3. Variance → $\frac{\sum (x_i - \bar{X})^2}{n-1} = s^2$

4. standard deviation → $\sqrt{s^2} = s$

- number of interval to achieve the main advantage of

tubular presentation (summarization) is (4-12)

- Width usually (5, 10, 15) calculate by upper limit - lower limit (interval continuous)

by upper limit - lower limit (interval discrete)
+1

- Real limit (upper limit +0.5, lower limit -0.5)

- Graphical presentation
 - line graph → time (temperature, birth, death)
 - Bar chart → for qualitative and quantitative discrete
 - Histogram → continuous quantitative (no space between columns)
 - Frequency polygon (midpoint of interval on X-axis)
 - pie chart (four type of variable) (12) ↻ clockwise

- parameter → numerical information about population.

- statistics → numerical information about sample.

- percentiles or quantiles = $np/100$

↓ 
أول خطوة رتب الأرقام في جدول ثم نصب على القانون $(np/100)$ نطلع رقم عشري أي بوه وطلعاه من الجدول وإذاطلع رقم صحيح يؤخذ رقم اللي بعده مكان و بروج على الجدول وبعد المتوسط للقيمين.

- Coefficient of variation → من أقل استقرار

$$CV = \frac{s}{\bar{x}} * 100\%$$

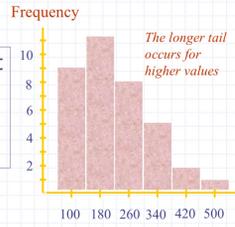
$CV \uparrow$ variance \uparrow stable, uniform \downarrow

- $SD \uparrow$ → wide / flat

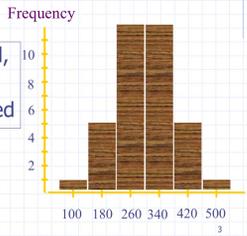
- $SD \downarrow$ → narrow / tall

SHAPES OF DISTRIBUTIONS

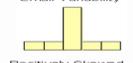
Skewed right
or
Positively skewed



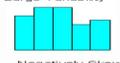
Symmetrical,
normal,
or bell-shaped



Unimodal
Small Variability



Bimodal
Large Variability



Positively Skewed



Kurtosis

Negatively Skewed



Large Kurtosis



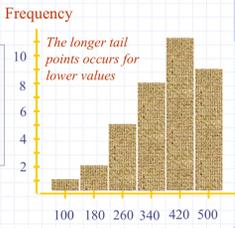
Little Kurtosis



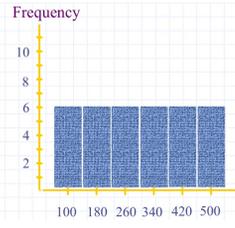
Symmetrical and possibly Normal



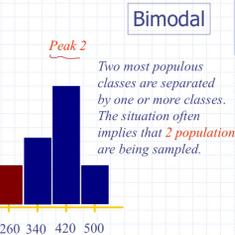
Skewed left
or
Negatively skewed



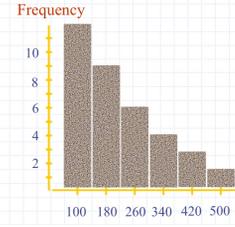
Uniform
or
rectangular



Bimodal



J-shaped



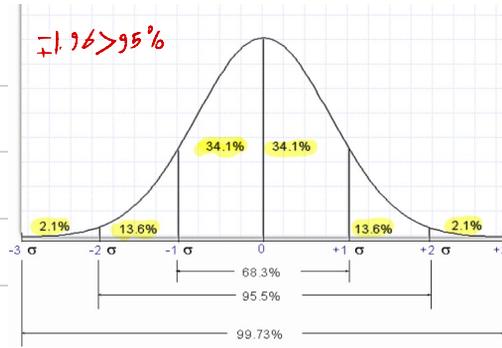
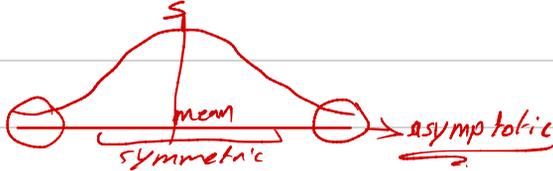
⇒ rare

- symmetrical \Leftrightarrow normal ^{normal} not normal But normal must be symmetrical
- frequency distribution maybe represented in the form graph (general variability and symmetry) and equation (and mean, median, mode) same location
- symmetry of variation is indicated by skewness
- tail of distribution indicated the type of skewness (right or left)
- Kurtosis \rightarrow flatness or peakedness
 - \rightarrow large \rightarrow high concentration on middle and out of tail
 - \rightarrow tilted \rightarrow high concentration on middle and thin in tail

- standard normal distribution

$\bar{X} = 0$ $SD = 1$

$Z = \frac{X - \bar{X}}{S}$

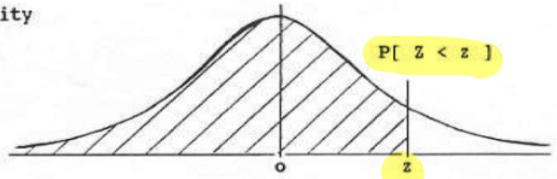


STANDARD STATISTICAL TABLES

1. Areas under the Normal Distribution

The table gives the cumulative probability up to the standardised normal value z i.e.

$P[Z < z] = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp(-\frac{1}{2}Z^2) dz$



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5159	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7854
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8804	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9773	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9865	0.9868	0.9871	0.9874	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
z	3.00	3.10	3.20	3.30	3.40	3.50	3.60	3.70	3.80	3.90
P	0.9986	0.9990	0.9993	0.9995	0.9997	0.9998	0.9998	0.9999	0.9999	1.0000

(Final)

- confidence intervals \rightarrow range of likely values for the parameter.

$$\left(\bar{X} + \frac{\alpha \sigma}{\sqrt{n}}, \bar{X} - \frac{\alpha \sigma}{\sqrt{n}} \right)$$

- likely value (true) \rightarrow critical values for standard normal distribution.

confidence coefficient \Rightarrow 95% $\alpha = 1.96$

\Rightarrow 90% $\alpha = 1.65$

\Rightarrow 99% $\alpha = 2.33$

- large sample \downarrow standard error

- Interval coefficient narrow \rightarrow more precise

- t-distribution \rightarrow bell shape (continuous data)

similar to z curve but \rightarrow degree of freedom (n-1)

\rightarrow wider tail

\rightarrow degree of freedom \uparrow approaches the standard normal distribution (on infinity)

- p-values \rightarrow chance

- statistical significance doesn't of necessity clinical significance

- Null hypothesis \rightarrow no difference (H_0)

- Alternative hypothesis \rightarrow have difference (H_1) (more or less) reject Null

- Type I error \rightarrow rejecting H_0 when H_0 true (α)

- Type II error \rightarrow accepting H_0 when H_1 true (β) (power of test)

-Hypothesis test \Rightarrow decide whether difference or no difference between sample

1. One-sample t-test

$$t = \frac{\bar{X} - \mu}{s/\sqrt{n}}$$

إذا كان معطى μ للكان population، نستخدم

2. Independent / Two-sample t-test

إذا كان معطى μ و σ أو μ و σ لغير المعين نستخدم

$$t = \frac{\bar{X}_1 - \bar{X}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$s^2_p = \frac{s_1^2(n_1-1) + s_2^2(n_2-1)}{n_1 + n_2 - 2}$

3. Dependent t-test (paired)

$$t = \frac{\bar{D} - \mu_0}{SD/\sqrt{n}}$$

إذا كان معطى عين قبل وبعد (before, after) نستخدم μ_0 (pre post) # $D \Rightarrow$ difference

* بعد إجراء اختبار بالبيانات t أو F نجد degree of freedom من $(n-1)$ من الجدول إذا كانت القيمة الحسابية أقل من القيمة الحرجة من جدول t أو F فإننا نقبل H_0 or fail to reject H_0 # لا يوجد اختلاف
فإنها إذا كانت القيمة الحسابية أكبر من القيمة الحرجة من الجدول t أو F فإننا نرفض H_0 / accept H_1 # يوجد اختلاف

4. Chi-square (χ^2) test (relation, contingency table)

$$E = \frac{\text{Total column} \times \text{total rows of cell}}{\text{Grand total}}$$

$$\chi^2 = \sum (O - E)^2$$

* إذا كانت χ^2 أكبر من α^2 فإننا نرفض H_0
* إذا كانت χ^2 أقل من α^2 فإننا نقبل H_0